

Performance of solenoids vs. quadrupoles in focusing and energy selection of laser accelerated protons.

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Using laser accelerated protons or ions for various applications - for example in particle therapy or short-pulse radiographic diagnostics - requires an effective method of focusing and energy selection. We derive an analytical scaling for the performance of a solenoid compared with a doublet/triplet as function of the energy, which is confirmed by TRACEWIN simulations. The scaling shows that above a few MeV a solenoid needs to be pulsed or super-conducting, whereas the quadrupoles can remain conventional. The transmission of the triplet is found only 25% lower than that of the equivalent solenoid. Both systems are equally suitable for energy selection based on their chromatic effect as is shown using an initial distribution following the RPA simulation model by Yan et al.[1].

I. INTRODUCTION

Laser acceleration of protons or ions requires ultra high laser intensities focused on thin target foils. This has been demonstrated in numerous experiments (see, for instance, Refs. [2–5]). Applications of this novel acceleration method have been suggested, for example in terms of a new proton source for radiation therapy [6–8] as alternative to more conventional accelerator technologies, like protons or ions from cyclotrons or synchrotrons. Other potential applications might be proton radiography, neutron imaging or isotope production. Energies up to 170 MeV for deuterons have recently been observed at the TRIDENT laser and explained as “break-out afterburner” (BOA) mechanism [9], with possible applications as very short-pulse neutron source.

All of these applications have to cope with the characteristics of laser accelerated protons or ions: a large energy spread as well as angular spread, sub-ns time scales, significant shot-to-shot fluctuations and - for practical applications - relatively low repetition rates compared with conventional accelerators. This requires specific methods to suitably manipulate laser accelerated protons in space and time and match them to the need of an experiment or application.

In a preceding study we have shown that a single solenoid magnet can be used very effectively to combine angular focusing (collection) with energy selection due to the lens chromatic effect [10]. This is extended here to a comparative evaluation of quadrupole focusing (doublet or triplet) and solenoid focusing. As in the solenoid case, we use the dependence of focal length on energy and employ a radially confining aperture to select a suitable energy window. The main difference of quadrupoles versus a solenoid is their first order focusing property (solenoids focus in second order) and the asymmetry in focusing (astigmatism) as well as different chromatic effects between the horizontal and vertical planes. On the other

hand alternating gradient focusing with quadrupoles is known to be more efficient at increasing energy and helps to avoid pulsed magnet or superconducting technology.

It should be mentioned here that the alternative to energy selection by the chromatic effect is the more conventional energy selection using the dispersive properties of dipole magnets. All therapy oriented studies on laser acceleration carried out in the course of the last years have used such a system with a collimating aperture followed by a dispersive dipole magnet [11–14]. Dispersive energy selection is certainly an option, but schemes without transverse focusing may result in significant efficiency loss. Chromatic energy selection, instead, combines the advantages of focusing with energy selection in a single device. However, for effective selection it is required that the beam size by chromaticity dominates over the size by the intrinsic emittance, which is not the case in many situations - but certainly for laser accelerated particles.

An interesting alternative is the micro-lens, which focusses by means of an electron plasma initialized by a second short-pulse laser beam and collapsing inside a cylinder [15]. Energy selection is enabled by using time-of-flight and triggering the second laser beam accordingly. For therapy applications, however, where energy selection failure cannot be tolerated, the fully controllable powering of conventional magnets for energy selection seems essential.

In Section II we compare solenoidal with doublet/triplet focusing. Their chromatic focusing properties are studied in Section III. In Section IV results are applied to energy selection by an aperture for both systems using an input distribution from the simulation of a radiation pressure acceleration model. In Section V we draw conclusions.

II. COMPARISON OF SOLENOIDAL AND QUADRUPOLE FOCUSING

Solenoids are frequently applied in injectors for focusing of particles with relatively low energy and large divergence. Likewise, focusing of laser accelerated protons with energies of the order of 10 MeV was demon-

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strated using a pulsed solenoid [16, 17]. Other laser proton experiments in a comparable energy range have successfully employed small aperture, high-gradient permanent magnet quadrupoles [18]. Preference of quadrupoles over solenoids depends on the individual application, but certainly energy and the question of room-temperature, non-pulsed quadrupoles versus pulsed or superconducting solenoids matter.

A useful guidance to decide on the basis of required field strengths can be obtained from a scaling expression using the thin lens approximations for the focal length f_s of a solenoid and F_d of a quadrupole doublet as suggested in Ref. [19]. With B the field strength (for the quadrupoles defined at the poles), and assuming that both focal lengths are defined from the respective centers, we have for the solenoid of length L

$$1/f_s \approx \left(\frac{q}{2mc\beta\gamma}\right)^2 B^2 L; \quad (1)$$

likewise for the doublet

$$1/F_d \approx \left(\frac{qB}{mc\beta\gamma a}\right)^2 l^2 s, \quad (2)$$

where l is the individual quadrupole length, s the separation of quadrupoles (from center to center) and a the maximum beam radius (pole radius). Note that the focal strength of a doublet increases with the separation of its components - of course on the expense of decreasing acceptance. Comparing a solenoid with a doublet of the same overall length L and equal field B , we readily obtain from Eqs. 1 and 2 the ratio T_d of focusing strengths (here defined as inverse focal lengths) in terms of only geometrical quantities:

$$T_d \equiv \frac{1/F_d}{1/f_s} = \frac{4sl^2}{a^2 L}, \quad (3)$$

Eq. 3 indicates that the focusing strength of a doublet is superior to that of a solenoid, if a is sufficiently small relative to the length. As an example, consider a doublet with a gap between magnets equal to their length, in which case we have $T_d = (2/3)^3 (L/a)^2$ and the transition condition $T_d > 1$ occurs for $L/a > (3/2)^{3/2}$.

In order to obtain systems with equivalent focal lengths it may be required to adjust B_s according to Eq. 1. This results in an effective field for the solenoid

$$B_s^* = T_d^{1/2} B_d, \quad (4)$$

which may lead to the requirement of super-conducting or pulsed power technologies for the solenoid.

We can apply this to the collection of laser particles, if we assume the focal spot is at the source and the beam is to be made parallel by the lens. In the interest of smoother focusing we find it preferable to use a triplet rather than a doublet as reference case. In Fig. 1 we show - as example - a triplet with $L = 0.334$ m, $l = 0.06$ m and gradients of 30 T/m, -30 T/m and 15 T/m. The

calculation of matched beam optics is obtained using the envelope option of the TRACEWIN code [20], which is also employed further below for particle tracking.

2 MeV protons with source divergence of ± 125 mrad are made parallel with a triplet focal length (source to triplet center) $F_t = 0.254$ m, maximum envelope $a = 48$ mm, hence maximum pole-tip field $B_t = 1.44$ T. Note that the distance source to lens is given by $F_t - L/2$, which is 87 mm in this case. The energy spread is assumed to be zero, which is to avoid the chromatic energy effect at this point. For comparison we also show a solenoid focusing with the same L ; in order to achieve the same focal length we require a slightly increased magnetic field $B_s = 1.53$ T. Next we check if our TRACEWIN results still obey the

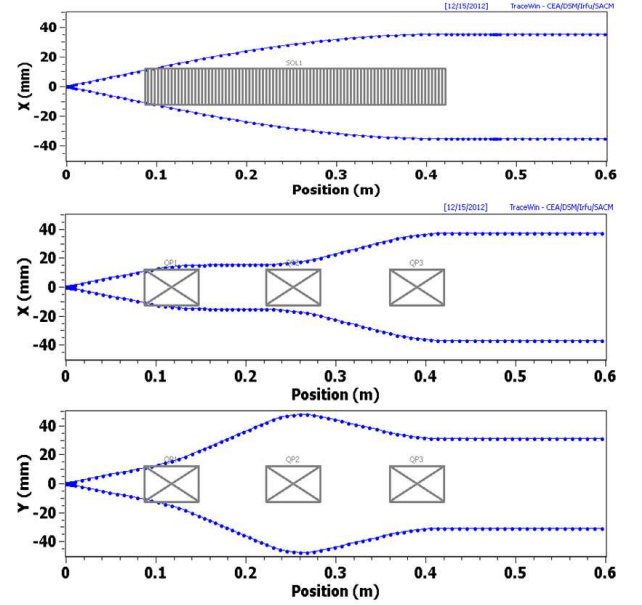


FIG. 1. TRACEWIN envelopes for equivalent triplet (top) and solenoid (bottom) solutions at 2 MeV.

scaling of Eq. 3, although we have replaced the doublet by a triplet. We find good agreement, if we replace $4s$ by $2s$. The need for this adjustment can be interpreted as necessary compensation of the (approximate) doubling of the triplet length compared with that of the doublet. This suggests a triplet focusing enhancement factor

$$T_t \equiv \frac{1/F_t}{1/f_s} = \frac{2sl^2}{a^2 L}. \quad (5)$$

Assuming that the gap equals the quadrupole length, we have $s = 2l$, which results in $T_t \approx 1.12$ in the above example. Applying Eq. 4 we find that the predicted solenoid field for equivalent focal length is 1.52 T, which agrees quite well with the above TRACEWIN result - in spite of the thin lens approximations employed in the derivation of T_t .

In order to further examine the validity of Eq. 5 for different energies we extend the systems in Fig. 1 to proton energies of 0.2, 20 and 200 MeV, again assuming

at each energy equal overall lengths L for solenoid and triplet, equal focal lengths for the two systems as well as equal gap and quadrupole lengths in the triplet case. For the initial divergence we assume - somewhat arbitrarily - a divergence scaling $x' \propto (\beta\gamma)^{-1/2}$ to account for the expected trend of decreasing divergence with energy. The value of x' at 2 MeV is kept as before. We first use TRACEWIN and search again for matched solutions requiring a parallel output beam for vanishing energy spread. In Table II we summarize all relevant parameters including the resulting quadrupole pole tip fields B_t and solenoid strengths B_s . The focal length F is again defined from source to center of the respective lens system and found to increase with energy. The theoretically expected triplet enhancement factor T_t is calculated from Eq. 5 ($s = 2l$) by inserting the respective geometrical dimensions. Using Eq. 4, which applies equally to the pole tip field of the triplet as it does for the doublet, we can thus derive the theoretically expected B_s^* and compare it with the actual B_s obtained from TRACEWIN matching. As result we find an overall good agreement between

E (MeV)	x'	L	F	l	a	B_t	B_s	T_t	B_s^*
0.2	400	25.0	22.5	2	5.3	1.60	0.59	0.046	0.34
2	125	33.4	25.4	6	4.8	1.44	1.53	1.12	1.52
20	71	62.0	47.0	10	4.8	1.50	2.62	2.8	2.51
200	39	108.0	79.0	20	4.5	1.35	5.10	14.6	5.16

TABLE I. Comparison simulation - theory for equivalent solenoid and triplet focusing properties; lengths in cm and magnetic fields in T (x' in mrad).

the TRACEWIN calculated B_s and the theoretical B_s^* , which confirms the theoretically derived triplet focusing enhancement over a solenoid. In Fig. 2 we summarize the main findings from this comparison.

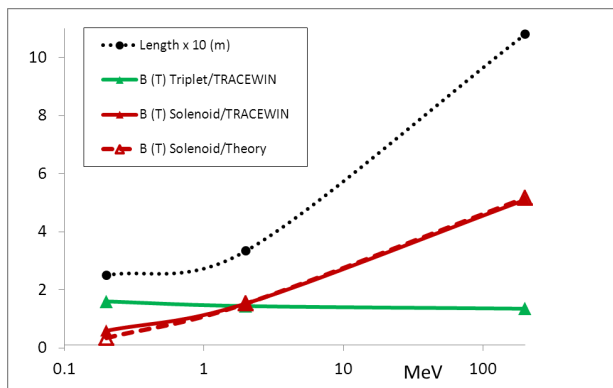


FIG. 2. Comparison of triplet and solenoid systems with equal focal lengths as function of energy.

In summary, this demonstrates that for sub-MeV or few MeV energies solenoids are a convenient approach, whereas the quadrupole doublet/triplet (or multiplet) has advantages for higher energies as its pole tip field strengths remain within iron saturation. Eq. 5 also sug-

gests that $T_t \propto 1/a^2$, hence larger a due to an increased initial divergence shifts the advantage of the doublet/triplet over the solenoid to higher energies - and vice versa.

III. CHROMATIC PROPERTIES OF SOLENOID AND TRIPLET

TRACEWIN is used here for particle tracking. Although primarily a linear accelerator design and verification tool, it has a number of features, which make the code suitable for our problem as well. In particular, it

- is a self-consistent 3D particle-in-cell code suitable for tracking of up to 10^7 simulation particles,
- is capable of energy dependent focussing (chromatic aberrations),
- includes field map options for magnetic elements (like solenoids) to model higher order (for example geometric) lens aberrations,
- provides standard 6D phase space initial distributions as well as user provided input distributions; as “standard uniform” we choose for this study the option of a uniform distribution in the 4D transverse space as well as uniform within the longitudinal phase plane ellipse;
- includes an envelope option for beam optics design.

Space charge options with 2D/3D Poisson solvers exist, but space charge is ignored in this study. In Ref. [10] it is shown for solenoids that space charge is generally weak; in the near-source region, where extremely high proton densities are prevailing, neutralization by the co-moving electrons helps.

In the following we use as reference a solenoid and an equivalent triplet, both 104 cm long and designed to bring 250 MeV protons to a focus at 2.73 m with the following assumptions:

- initial maximum divergence angle: ± 28 mrad
- energy spread: practically mono-energetic
- distance laser target - first magnet: 35 cm
- beam pipe radius: 3.5 cm
- aperture radius of solenoids and quadrupoles: 3 cm
- length of solenoid field map: 104 cm
- length of solenoid field region: 80 cm
- averaged solenoid field 6.27 T
- length of solenoid field map: 96 cm
- length of quadrupoles: 15 cm

- quadrupole pole tip fields: 1.5/1.5/1.0 T

Fig. 3 shows density plots from a multi-particle simulation using a low number of simulation particles (only 3000), which helps to visualize single particle rays. The simulation was carried out with the “standard uniform” initial distribution of TRACEWIN. Maximum energy deviations in this example have been chosen as $\pm 5 \times 10^{-4}$ MeV centered at 250 MeV, hence practically mono-energetic. The common waist for x and y for the triplet (stigmatic image) is relevant for optimum energy selection as will be shown in the next section. It is noticed

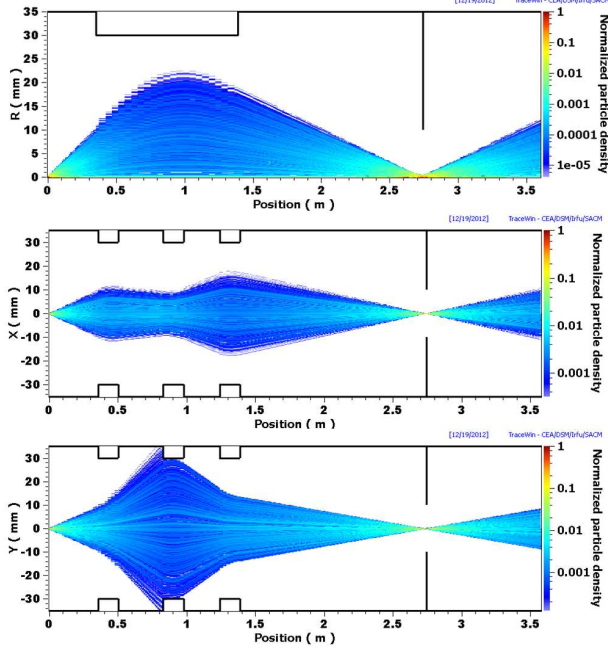


FIG. 3. Density plots for TRACEWIN obtained reference cases for “equivalent” solenoid (top) and triplet (center: x and bottom: y) focusing.

that the de-focusing effect of the first quadrupole in y leads to a - in this example - small beam loss at the aperture of the second quadrupole.

In Refs. [10] the energy dependence of the focal length of a solenoid lens was expressed in terms of a chromatic coefficient, which we generalize here to cope with the different focusing in x and y for a triplet:

$$\alpha_{x,y} \equiv \frac{\delta f_{x,y}/f_{x,y}}{\delta E/E}. \quad (6)$$

Here $f_{x,y}$ is the focal length at the reference energy E and $\alpha_{x,y}$ is specific to the geometry of the focusing setup. For the examples of Fig. 3 we find from TRACEWIN simulation for the solenoid $\alpha_r \approx 1.9$ and for the triplet $\alpha_x \approx 0.9$ as well as $\alpha_y \approx 3.8$. The much larger α_y is a result of the de-focusing in y at the first lens and the thus much larger overall envelope excursions in y . The solenoid chromatic coefficient is - not surprisingly - close

to the geometrical mean of the two coefficients for the equivalent triplet.

The chromatic effect is strongly correlated with time as higher energy particles travel ahead. The stronger focusing for lower energies leads to an enhanced transverse phase space rotation of protons at the bunch end as compared with the high energy particles at the bunch head. The resulting slip in the transverse phase planes causes an effective transverse emittance increase, which can significantly exceed the initially small production emittance. The effective emittance is obtained by averaging the instantaneous emittances over the full bunch length, hence the full energy spectrum [10].

IV. TRANSMISSION AND ENERGY SELECTION

As suggested in Refs. [10] the pronounced chromatic focusing effect can be used for an effective energy selection, if the beam is focused into a suitably defined transverse aperture. Only particles with focal spot sufficiently close to the aperture plane are transmitted effectively. As for solenoids this works effectively only if the beam is “chromaticity dominated”: at a selection aperture the beam size by chromaticity dominates over the size generated by the intrinsic emittance at any relevant value of the energy (i.e. position along the bunch). This is always the case for laser generated ions with their extremely small emittance at any given energy, which is owed to the very small source spot size. It should be mentioned here that the intrinsic emittance should also include emittance increase due to higher order aberrations of the lens, which can be a problem for short solenoid lenses at low energy but is not further considered in this study.

A. RPA generated initial distribution

For practical considerations it is advantageous to consider an initial distribution in 6D phase space with a broadened energy distribution according to some laser acceleration model. The Radiation Pressure Acceleration (RPA) mechanism [21–26] has a high potential to reach proton energies of hundreds of MeV. A specific theoretical version of it has been discussed in Ref. [1] and applied to proton therapy conditions in Refs. [10, 27] to create a proton energy spectrum extending up to 250 MeV. The output of this RPA-simulation can be described as spectral yield

$$\frac{dN(E, \Omega)}{dE} [MeV^{-1}], \quad (7)$$

which describes the number of particles in an energy interval dE and within a cone angle $\pm\Omega$. The thus defined proton spectrum (details see Ref. [27]) is plotted in Fig. 4. Its energy distribution is peaked above 200 MeV - determined by the laser intensity - with a relatively broad foot

towards lower energies. As input into our TRACEWIN simulations we take a bi-Gaussian approximation to this energy spectrum shown by the continuous curve in Fig. 4. The 6D initial distribution is taken as a Gaussian random distribution in the variables t, x, x', y, y' . For the rms widths in x', y' we have chosen 35 mrad - in contrast with the broader tails in divergence indicated in Fig. 4, which are probably due to the 2D nature of the RPA simulation. The initial spot radius and pulse duration are in the μm resp. ps scales; their actual values play no role as long as space charge is considered as neutralized initially. We also note that the detailed profile of the energy spectrum is only exemplary - what matters primarily is its gradient near a selected energy.

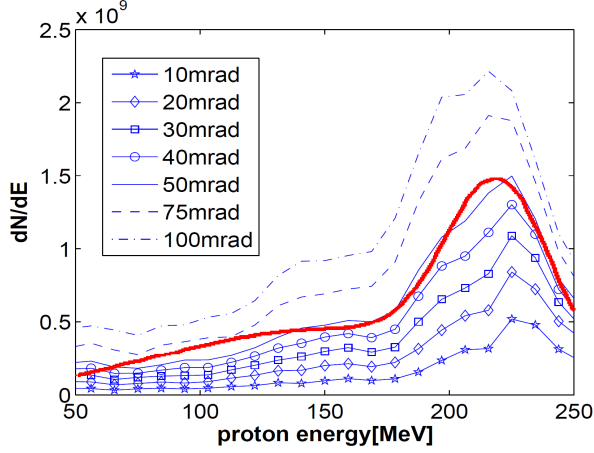


FIG. 4. Spectral yield of protons as a function of energy and for different capture cone angles Ω , with bi-Gaussian fit (continuous line).

B. Comparative transmission

For this purpose we reduce the magnet fields in the equivalent solenoid and triplet systems of Fig. 3 for nominal transmission at 220 MeV, which is closer to the peak of the energy spectrum. We also require - arbitrarily - a focus at the distance of 2.73 m from the laser target, where the energy selection aperture is placed. Employing the above defined RPA-distribution and a 3 mm radius aperture, the resulting orbits of a TRACEWIN simulation with 3000 rays are shown in Fig. 5. In Fig. 6 we examine the transverse emittances for the triplet of Fig. 5. The relatively large spread in x', y' and energy width together with the energy dependent focusing result in significant emittance growth in x and y within the quadrupoles, accompanied by emittance reductions due to beam loss on the radial aperture. Note that emittances are understood here as averaged over the full bunch length, while the “instantaneous” emittances at a given position along the expanding bunch remain at their small initial values. The emittance reduction in y within

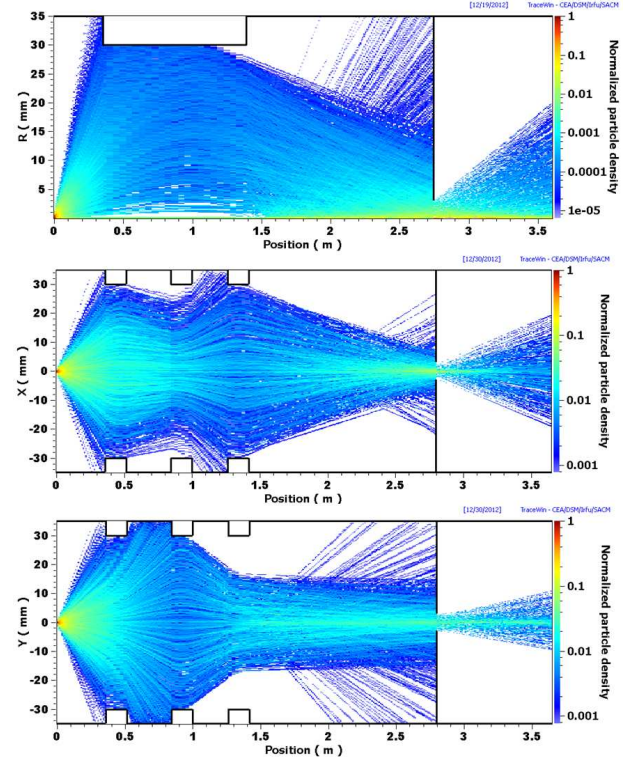


FIG. 5. Density plots for RPA-distribution in equivalent solenoid (top) and triplet (center: x and bottom: y) systems adjusted to 220 MeV.

the first quadrupole reflects the beam loss in the defocusing y -direction. A comparison of the equivalent solenoid

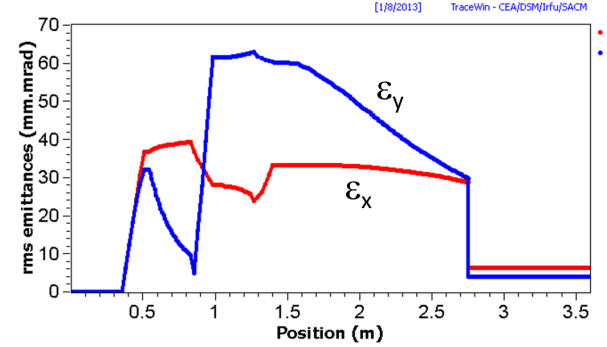


FIG. 6. Transverse (normalized and bunch averaged) rms emittances for triplet case.

and triplet focusing systems shows that the overall transmission for the solenoid is 47%, and 35% for the triplet. The corresponding loss profiles are shown in Fig. 7. The beam loss in y in the first lens of the triplet is to some extent compensated by an enhanced transmission in x , which explains why the triplet transmission is only 25% lower than the solenoid one. A more differentiated insight is gained, if we truncate the divergence of the initial Gaussian distribution in x', y' by eliminating all particles

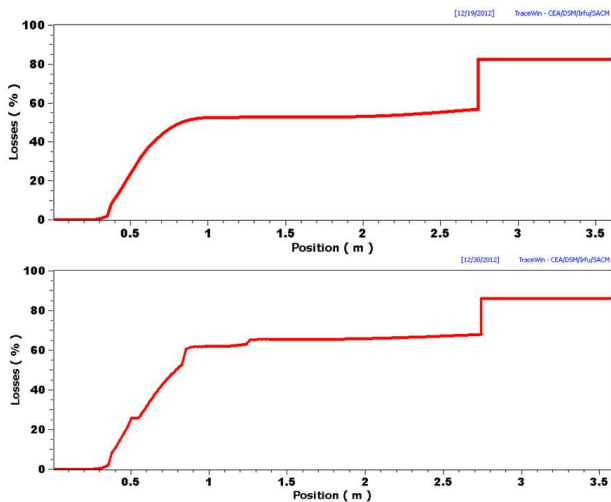


FIG. 7. Loss profiles for RPA-distributions in the equivalent solenoid (top) and triplet (bottom).

beyond a “divergence limit” as shown in Fig. 8. Below about 40 mrad the solenoid accepts all injected particles in the truncated distribution (intensity in it relative to un-truncated distribution indicated by the dotted line); at this value the acceptance limit is reached and larger divergence particles are lost. The triplet, instead, starts losing particles above 20 mrad, but the transition to its acceptance limit is smoother - apparently due to the benefit from the horizontal plane.

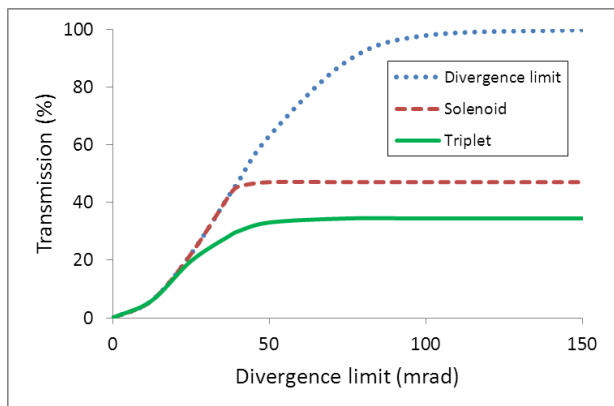


FIG. 8. Transmission of solenoid and triplet as function of an upper cut-off (divergence limit) of the injected particles. The transmission is in % of the particles in the original un-truncated distribution.

C. Selection of energies

Following Ref. [10] the radius of a selection aperture is proportional to the product of required energy width

and chromatic coefficient α ,

$$R_A = \alpha \frac{\Delta E}{E} A_{max}, \quad (8)$$

where A_{max} is the maximum envelope at the lens. Using $A_{max} \approx 3$ cm and $\alpha \approx 2$ we expect that an energy width of $\pm 4\%$ (± 8.8 MeV) should be obtainable with an aperture of 2.4 mm radius. This is approximately confirmed by the energy spectra in Fig. 9, where R_A was chosen as 3 mm for the solenoid and 2.7 mm for the triplet to reach the same fwhm width. The overall yield in the

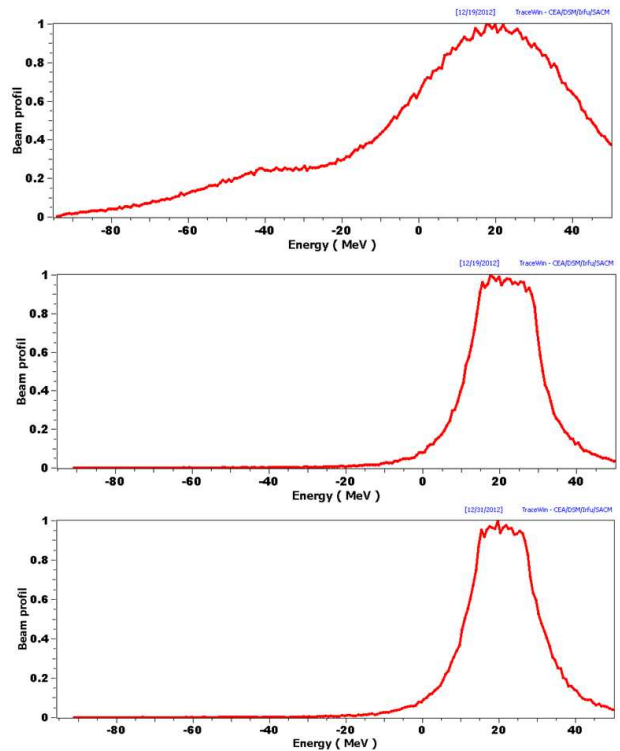


FIG. 9. Selected energy spectra for equivalent solenoid ($R_A = 3$ mm) and triplet systems ($R_A = 2.7$ mm). Top: initial; center: solenoid; bottom: triplet.

selected energy windows is 17% for the solenoid and 13 % for the triplet, which follows approximately the 25% triplet transmission reduction found in Fig. 8.

For the triplet we have also simulated an elliptical selection aperture in x, y with the same area but semi-axes in the ratio 1:4 to match the ratio of chromatic coefficients according to Eq. 8. However, we obtain practically the same energy selection width and profile as well as transmission. This seems somewhat unexpected, but apparently the loss of selection in one plane is compensated by better selection in the other plane.

V. CONCLUSION

The purpose of this study has been a comparative assessment of the focusing properties of a solenoid and a

quadrupole triplet in the context of laser accelerated protons (or ions). Possible application of this acceleration method can be envisioned in the field of particle therapy; but also in proton radiography in areas, where energies of a few hundred MeV, moderate integrated intensities but high peak intensities in time-scales of few ns or sub-ns are needed. The relatively large initial angular and energy spreads are a challenge for all of these applications.

In terms of transmission it is found that “equivalent” systems - same geometrical length and apertures - give only the relatively small reduction in transmission of 25% for the triplet vs. the solenoid, which is owed to the un-symmetric focusing of quadrupoles. For increasing energies - already above a few MeV - the weaker focusing properties of solenoids require pulsed or superconducting technology, whereas pole-tip fields of a doublet or triplet can remain within room-temperature iron saturation. This appears to be a clear advantage for quadrupoles in future therapy applications, where short-term and fully controlled changes of energy and magnetic

rigidity are required.

The large energy spreads lead to a dominance of chromatic effects, which can be used for energy selection. Equivalent solenoid and triplet systems are equally suitable for this purpose in spite of the strongly differing chromatic coefficients in x and y . Chromatic effects lead to inevitable correlations between energy and transverse position, which cannot be ignored for therapy applications. In Ref. [10] it is shown that properly placed scatter targets can be used to remove these correlations.

The role of space charge and geometric aberrations - dominant for short solenoids - needs further consideration even though they are not expected to alter the major conclusions. Noting that solenoid focusing is independent of the charge, the neutralizing co-moving electrons, which are always present in laser acceleration, will be strongly focussed towards the axis [28]. In the triplet, instead, these electrons will be de-focussed to the aperture when entering the first quadrupole, which may have an effect on the quality of focusing and needs to be further explored.

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